Scipy.org (https://scipy.org/) Docs (https://docs.scipy.org/)
NumPy v1.17 Manual (https://docs.scipy.org/doc/numpy/index.html)
NumPy User Guide (https://docs.scipy.org/doc/numpy/user/index.html)
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## NumPy for Matlab users

## Introduction

MATLAB® and NumPy/SciPy have a lot in common. But there are many differences. NumPy and SciPy were created to do numerical and scientific computing in the most natural way with Python, not to be MATLAB® clones. This page is intended to be a place to collect wisdom about the differences, mostly for the purpose of helping proficient MATLAB® users become proficient NumPy and SciPy users.

## Some Key Differences

In MATLAB®, the basic data type is a multidimensional array of double precision floating point numbers. Most expressions take such arrays and return such arrays. Operations on the 2-D instances of these arrays are designed to act more or less like matrix operations in linear algebra.
MATLAB® uses 1 (one) based indexing. The initial element of a sequence is found using a(1). See note INDEXING
MATLAB®'s scripting language was created for doing linear algebra. The syntax for basic matrix operations is nice and clean, but the API for adding GUIs and making full-fledged applications is more or less an afterthought.

In MATLAB®, arrays have pass-by-value semantics, with a lazy copy-on-write scheme to prevent actually creating copies until they are actually needed. Slice operations copy parts of the array.

In NumPy the basic type is a multidimensional array. Operations on these arrays in all dimensionalities including 2D are element-wise operations. One needs to use specific functions for linear algebra (though for matrix multiplication, one can use the @ operator in python 3.5 and above).

Python uses 0 (zero) based indexing. The initial element of a sequence is found using a[0].
NumPy is based on Python, which was designed from the outset to be an excellent general-purpose programming language. While Matlab's syntax for some array manipulations is more compact than NumPy's, NumPy (by virtue of being an add-on to Python) can do many things that Matlab just cannot, for instance dealing properly with stacks of matrices.

In NumPy arrays have pass-by-reference semantics. Slice operations are views into an array.

## 'array' or 'matrix'? Which should I use?

Historically, NumPy has provided a special matrix type, np.matrix, which is a subclass of ndarray which makes binary operations linear algebra operations. You may see it used in some existing code instead of np.array. So, which one to use?

## Short answer

## Use arrays

- They are the standard vector/matrix/tensor type of numpy. Many numpy functions return arrays, not matrices.
- There is a clear distinction between element-wise operations and linear algebra operations.
- You can have standard vectors or row/column vectors if you like.

Until Python 3.5 the only disadvantage of using the array type was that you had to use dot instead of $*$ to multiply (reduce) two tensors (scalar product, matrix vector multiplication etc.). Since Python 3.5 you can use the matrix multiplication @ operator.

Given the above, we intend to deprecate matrix eventually.

## Long answer

NumPy contains both an array class and a matrix class. The array class is intended to be a general-purpose $n$-dimensional array for many kinds of numerical computing, while matrix is intended to facilitate linear algebra computations specifically. In practice there are only a handful of key differences between the two.

- Operators * and @, functions dot(), and multiply():
- For array, "*"` means element-wise multiplication, while " @"` means matrix multiplication; they have associated functions multiply() and dot (). (Before python 3.5, @ did not exist and one had to use dot () for matrix multiplication).
- For matrix, ' "*` means matrix multiplication, and for element-wise multiplication one has to use the multiply() function.
- Handling of vectors (one-dimensional arrays)
- For array, the vector shapes $1 \times N, N x 1$, and $N$ are all different things. Operations like $\mathrm{A}[:, 1]$ return a onedimensional array of shape N , not a two-dimensional array of shape Nx 1 . Transpose on a one-dimensional array does nothing.
- For matrix, one-dimensional arrays are always upconverted to $1 \times N$ or Nx 1 matrices (row or column vectors). A[:,1] returns a two-dimensional matrix of shape Nx 1
- Handling of higher-dimensional arrays (ndim >2)
- array objects can have number of dimensions $>2$;
- matrix objects always have exactly two dimensions.
- Convenience attributes
- array has a .T attribute, which returns the transpose of the data.
- matrix also has .H, .I, and .A attributes, which return the conjugate transpose, inverse, and asarray () of the matrix, respectively.
- Convenience constructor
- The array constructor takes (nested) Python sequences as initializers. As in, array ([ [1, 2, 3] , [4, 5, 6] ]).
- The matrix constructor additionally takes a convenient string initializer. As in matrix("[1 2 3; 4 5 6]").

There are pros and cons to using both:

- array
- :) Element-wise multiplication is easy: $A * B$.
- : ( You have to remember that matrix multiplication has its own operator, @.
- :) You can treat one-dimensional arrays as either row or column vectors. A @ v treats vas a column vector, while v @ A treats $v$ as a row vector. This can save you having to type a lot of transposes.
- :) array is the "default" NumPy type, so it gets the most testing, and is the type most likely to be returned by 3rd party code that uses NumPy.
- :) Is quite at home handling data of any number of dimensions.
- :) Closer in semantics to tensor algebra, if you are familiar with that.
- : ) Alloperations (*, /, +, - etc.) are element-wise.
- : ( Sparse matrices from scipy. sparse do not interact as well with arrays.
- matrix
- $: \backslash \backslash$ Behavior is more like that of MATLAB® matrices.
- <: ( Maximum of two-dimensional. To hold three-dimensional data you need array or perhaps a Python list of matrix.
- <: ( Minimum of two-dimensional. You cannot have vectors. They must be cast as single-column or single-row matrices.
- <: ( Since array is the default in NumPy, some functions may return an array even if you give them a matrix as an argument. This shouldn't happen with NumPy functions (if it does it's a bug), but 3rd party code based on NumPy may not honor type preservation like NumPy does.
- :) A*B is matrix multiplication, so it looks just like you write it in linear algebra (For Python >= 3.5 plain arrays have the same convenience with the @ operator).
- < : ( Element-wise multiplication requires calling a function, multiply (A,B).
- < : ( The use of operator overloading is a bit illogical: * does not work element-wise but / does.
- Interaction with scipy.sparse is a bit cleaner.

The array is thus much more advisable to use. Indeed, we intend to deprecate matrix eventually.

## Table of Rough MATLAB-NumPy Equivalents

The table below gives rough equivalents for some common MATLAB® expressions. These are not exact equivalents, but rather should be taken as hints to get you going in the right direction. For more detail read the built-in documentation on the NumPy functions.

In the table below, it is assumed that you have executed the following commands in Python:
from numpy import *
import scipy.linalg

Also assume below that if the Notes talk about "matrix" that the arguments are two-dimensional entities.

## General Purpose Equivalents

| MATLAB | numpy | Notes |  |
| :--- | :--- | :--- | :--- |
| help func | info(func) or help(func) or func? <br> lpython) | (in | get help on the function func |
| which func | see note HELP <br> (https://docs.scipy.org/doc/numpy/user/numpy-for- <br> matlab-users.notes) | find out where func is defined |  |
| type func | source(func) or func?? (in lpython) | print source for func (if not a <br> native function) |  |
| a \&\& b | a and b | short-circuiting logical AND <br> operator (Python native <br> operator); scalar arguments <br> only |  |
| a \\| b | a or b | short-circuiting logical OR <br> operator (Python native <br> operator); scalar arguments <br> only |  |


| MATLAB | numpy | Notes |
| :--- | :--- | :--- |
| $1 * \mathrm{i}, 1^{*} \mathrm{j}, 1 \mathrm{li}, 1 \mathrm{j}$ | 1 j | complex numbers |
| eps | np.spacing(1) | Distance between 1 and the <br> nearest floating point number. |
| ode45 | scipy.integrate.solve_ivp(f) | integrate an ODE with Runge- <br> Kutta 4,5 |
| ode15s | scipy.integrate.solve_ivp(f, method='BDF') | integrate an ODE with BDF <br> method |
|  |  |  |

## Linear Algebra Equivalents

| MATLAB | NumPy | Notes |
| :---: | :---: | :---: |
| ndims(a) | ndim(a) or a.ndim | get the number of dimensions of an array |
| numel ( a ) | size(a) or a.size | get the number of elements of an array |
| size(a) | shape(a) or a.shape | get the "size" of the matrix |
| size(a, n ) | a.shape[n-1] | get the number of elements of the $n$-th dimension of array a . (Note that MATLAB® uses 1 based indexing while Python uses 0 based indexing, See note INDEXING) |
| [ 1 2 3; 4 5 6 ] | $\operatorname{array}([[1 ., 2 ., 3],.[4 ., 5 ., 6]]$. | 2x3 matrix literal |
| [ a b; c d ] | block([[a, b], [c,d]]) | construct a matrix from blocks $a, b, c$, and d |
| a (end) | a [-1] | access last element in the 1 xn matrix a |
| $a(2,5)$ | a $[1,4]$ | access element in second row, fifth column |
| $a(2,:)$ | $a[1]$ or a[1,:] | entire second row of a |
| a(1:5,:) | $a[0: 5]$ or $a[: 5]$ or $\mathrm{a}[0: 5,:]$ | the first five rows of a |
| a (end-4:end, : | a[-5:] | the last five rows of a |
| a(1:3,5:9) | a[0:3][:,4:9] | rows one to three and columns five to nine of a . This gives read-only access. |
| $a([2,4,5],[1,3])$ | a[ix_([1,3,4],[0,2])] | rows 2,4 and 5 and columns 1 and 3 . This allows the matrix to be modified, and doesn't require a regular slice. |
| a(3:2:21,:) | a[ 2:21:2,:] | every other row of a , starting with the third and going to the twenty-first |
| a(1:2:end,:) | a[ ::2,:] | every other row of a , starting with the first |
| a(end:-1:1,:) or flipud(a) | a[ : : - 1,: ] | a with rows in reverse order |
| a([1:end 1],:) | $a\left[r_{\sim}[: \operatorname{len}(\mathrm{a}), 0]\right.$ ] | a with copy of the first row appended to the end |
| a.' | a.transpose() or a.T | transpose of a |
| $a^{\prime}$ | a.conj().transpose() or a.conj().T | conjugate transpose of a |
| a*b | a @ b | matrix multiply |
| a .* b | $a * b$ | element-wise multiply |
| a./b | a/b | element-wise divide |
| a.^3 | a**3 | element-wise exponentiation |
| ( $\mathrm{a}>0.5$ ) | ( $\mathrm{a}>0.5$ ) | matrix whose $i, j t h$ element is (a_ij > 0.5). The Matlab result is an array of 0 s and 1 s . The NumPy result is an array of the boolean values False and True. |
| find( $\mathrm{a}>0.5$ ) | nonzero ( $\mathrm{a}>0.5$ ) | find the indices where (a) $0.5)$ |
| $\mathrm{a}(:, \mathrm{find}(\mathrm{v}>0.5))$ | a[: , nonzero(v>0.5)[0]] | extract the columms of a where vector v>0.5 |
| $\mathrm{a}(:, \mathrm{find}(\mathrm{v}>0.5))$ | $a[:, v . T>0.5]$ | extract the columms of a where column vector $v>0.5$ |
| $a(a<0.5)=0$ | $a[a<0.5]=0$ | a with elements less than 0.5 zeroed out |
| a .* (a>0.5) | a * (a>0.5) | a with elements less than 0.5 zeroed out |


| MATLAB | NumPy | Notes |
| :---: | :---: | :---: |
| $a(:)=3$ | a [:] $=3$ | set all values to the same scalar value |
| $y=x$ | $y=x \cdot \operatorname{copy}()$ | numpy assigns by reference |
| $y=x(2,:)$ | $y=x[1,:] \cdot \operatorname{copy}()$ | numpy slices are by reference |
| $y=x(:)$ | $\mathrm{y}=\mathrm{x} . \mathrm{flatten}()$ | turn array into vector (note that this forces a copy) |
| 1:10 | arange(1.,11.) or r_[1.:11.] or r_[1:10:10j] | create an increasing vector (see note RANGES) |
| 0:9 | arange(10.) or $r_{-}[: 10$.$] or$ r_[:9:10j] | create an increasing vector (see note RANGES) |
| [1:10]' | arange(1.,11.) [:, newaxis] | create a column vector |
| zeros (3,4) | $z \operatorname{eros}((3,4))$ | $3 \times 4$ two-dimensional array full of 64-bit floating point zeros |
| zeros (3,4,5) | zeros( $(3,4,5)$ ) | $3 \times 4 \times 5$ three-dimensional array full of 64-bit floating point zeros |
| ones ( 3,4 ) | ones( ( 3,4 ) | $3 \times 4$ two-dimensional array full of 64-bit floating point ones |
| eye(3) | eye(3) | $3 \times 3$ identity matrix |
| diag(a) | diag(a) | vector of diagonal elements of a |
| $\operatorname{diag}(\mathrm{a}, 0)$ | diag (a, 0) | square diagonal matrix whose nonzero values are the elements of a |
| rand ( 3,4 ) | random. rand $(3,4)$ or random.random_sample( $(3,4))$ | random $3 \times 4$ matrix |
| linspace(1,3,4) | linspace(1,3,4) | 4 equally spaced samples between 1 and 3 , inclusive |
| $[x, y]=m e s h g r i d(0: 8,0: 5)$ | mgrid[0:9.,0:6.] or meshgrid(r_[0:9.],r_[0:6.] | two 2D arrays: one of $x$ values, the other of $y$ values |
|  | $\begin{aligned} & \text { ogrid[0:9., 0:6.] or } \\ & \text { ix_(r_[0:9.],r_[0:6.] } \end{aligned}$ | the best way to eval functions on a grid |
| $[x, y]=m e s h g r i d([1,2,4],[2,4,5])$ | meshgrid([1,2,4],[2,4,5]) |  |
|  | ix_([1,2,4],[2,4,5]) | the best way to eval functions on a grid |
| repmat (a, m, n) | tile(a, (m, n) ) | create $m$ by n copies of a |
| [a b] | ```concatenate((a,b),1) or hstack((a,b)) or column_stack((a,b)) or c_[a,b]``` | concatenate columns of a and b |
| [a; b] | concatenate(( $a, b)$ ) or vstack((a,b)) or r_[a,b] | concatenate rows of $a$ and $b$ |
| $\max (\max (\mathrm{a})$ ) | a.max() | maximum element of $a$ (with ndims(a) $<=2$ for matlab) |
| $\max (\mathrm{a})$ | a.max (0) | maximum element of each column of matrix a |
| $\max (\mathrm{a},[\mathrm{l}, 2)$ | a. $\max (1)$ | maximum element of each row of matrix a |
| $\max (\mathrm{a}, \mathrm{b})$ | maximum(a, b) | compares $a$ and $b$ elementwise, and returns the maximum value from each pair |
| norm(v) | sqrt(v @ v) or np.linalg.norm(v) | L2 norm of vector v |
| $a \& b$ | logical_and (a,b) | element-by-element AND operator (NumPy ufunc) See note LOGICOPS |
| a \| b | logical_or(a, b) | element-by-element OR operator (NumPy ufunc) See note LOGICOPS |
| bitand (a, b) | $a \& b$ | bitwise AND operator (Python native and NumPy ufunc) |
| bitor (a, b) | a \| b | bitwise OR operator (Python native and NumPy ufunc) |
| inv (a) | linalg.inv(a) | inverse of square matrix a |
| pinv (a) | linalg.pinv(a) | pseudo-inverse of matrix a |
| rank(a) | linalg.matrix_rank(a) | matrix rank of a 2D array / matrix a |
| $a \backslash b$ | linalg.solve( $a, b$ ) if $a$ is square; linalg.lstsq(a,b) otherwise | solution of $\mathrm{a} \times \mathrm{x}$ b for x |
| b/a | Solve a.T $\times . T=$ b.T instead | solution of $\mathrm{xa}=\mathrm{b}$ for x |
| $[\mathrm{U}, \mathrm{S}, \mathrm{V}]=\operatorname{svd}(\mathrm{a})$ | U, S, Vh = linalg.svd(a), V = Vh.T | singular value decomposition of a |


| MATLAB | NumPy | Notes |
| :---: | :---: | :---: |
| chol (a) | linalg.cholesky(a).T | cholesky factorization of a matrix (chol (a) in matlab returns an upper triangular matrix, but linalg.cholesky(a) returns a lower triangular matrix) |
| [ V, D] =eig ( a ) | $\mathrm{D}, \mathrm{V}=$ linalg.eig(a) | eigenvalues and eigenvectors of a |
| [ V, D] $=$ eig ( $\mathrm{a}, \mathrm{b}$ ) | D,V = scipy.linalg.eig ( $\mathrm{a}, \mathrm{b}$ ) | eigenvalues and eigenvectors of a , b |
| [ V, D] $=$ eigs ( $\mathrm{a}, \mathrm{k}$ ) |  | find the $k$ largest eigenvalues and eigenvectors of a |
| $[Q, R, P]=q r(a, 0)$ | Q, $\mathrm{R}=$ scipy.linalg.qr(a) | QR decomposition |
| $[L, U, P]=\operatorname{lu}(a)$ | $L, U=$ scipy.linalg.lu(a) or LU, P=scipy.linalg.lu_factor(a) | LU decomposition (note: $P($ Matlab $)==$ transpose(P(numpy)) ) |
| conjgrad | scipy.sparse.linalg.cg | Conjugate gradients solver |
| fft(a) | fft(a) | Fourier transform of a |
| ifft(a) | ifft(a) | inverse Fourier transform of a |
| sort(a) | sort(a) or a.sort() | sort the matrix |
| [b,I] = sortrows $(a, i)$ | $\mathrm{I}=\operatorname{argsort}(\mathrm{a}[:, \mathrm{i}]), \mathrm{b}=\mathrm{a}[\mathrm{I},:]$ | sort the rows of the matrix |
| regress ( $\mathrm{y}, \mathrm{X}$ ) | linalg.lstsq(X,y) | multilinear regression |
| decimate(x, q) | scipy.signal.resample(x, len(x)/q) | downsample with low-pass filtering |
| unique(a) | unique (a) |  |
| squeeze(a) | a.squeeze() |  |

## Notes

Submatrix: Assignment to a submatrix can be done with lists of indexes using the ix_command. E.g., for 2d array a, one might do: ind=[1,3]; a[np.ix_(ind,ind)]+=100.

HELP: There is no direct equivalent of MATLAB's which command, but the commands help and source will usually list the filename where the function is located. Python also has an inspect module (do import inspect) which provides a getfile that often works.

INDEXING: MATLAB® uses one based indexing, so the initial element of a sequence has index 1. Python uses zero based indexing, so the initial element of a sequence has index 0 . Confusion and flamewars arise because each has advantages and disadvantages. One based indexing is consistent with common human language usage, where the "first" element of a sequence has index 1 . Zero based indexing simplifies indexing
(https://groups.google.com/group/comp.lang.python/msg/1bf4d925dfbf368?q=g:thl3498076713d\&hl=en). See also a text by prof.dr. Edsger W. Dijkstra (https://www.cs.utexas.edu/users/EWD/transcriptions/EWD08xx/EWD831.html).

RANGES: In MATLAB®, 0:5 can be used as both a range literal and a 'slice' index (inside parentheses); however, in Python, constructs like 0:5 can only be used as a slice index (inside square brackets). Thus the somewhat quirky $r$ _ object was created to allow numpy to have a similarly terse range construction mechanism. Note that $r_{-}$is not called like a function or a constructor, but rather indexed using square brackets, which allows the use of Python's slice syntax in the arguments.

LOGICOPS: \& or | in NumPy is bitwise AND/OR, while in Matlab \& and | are logical AND/OR. The difference should be clear to anyone with significant programming experience. The two can appear to work the same, but there are important differences. If you would have used Matlab's \& or | operators, you should use the NumPy ufuncs logical_and/logical_or. The notable differences between Matlab's and NumPy's \& and | operators are:

- Non-logical \{0,1\} inputs: NumPy's output is the bitwise AND of the inputs. Matlab treats any non-zero value as 1 and returns the logical AND. For example ( $3 \& 4$ ) in NumPy is 0 , while in Matlab both 3 and 4 are considered logical true and ( $3 \& 4$ ) returns 1.
- Precedence: NumPy's \& operator is higher precedence than logical operators like < and >; Matlab's is the reverse.

If you know you have boolean arguments, you can get away with using NumPy's bitwise operators, but be careful with parentheses, like this: $z=(x>1) \&(x<2)$. The absence of NumPy operator forms of logical_and and logical_or is an unfortunate consequence of Python's design.

RESHAPE and LINEAR INDEXING: Matlab always allows multi-dimensional arrays to be accessed using scalar or linear indices, NumPy does not. Linear indices are common in Matlab programs, e.g. find() on a matrix returns them, whereas NumPy's find behaves differently. When converting Matlab code it might be necessary to first reshape a matrix to a linear sequence, perform some indexing operations and then reshape back. As reshape (usually) produces views onto the same storage, it should be possible to do this fairly efficiently. Note that the scan order used by reshape in NumPy defaults to the ' $C$ ' order, whereas Matlab uses the Fortran order. If you are simply converting to a linear sequence and back this doesn't matter. But if you are converting reshapes from Matlab code which relies on the scan order, then this Matlab code: $z=$ reshape $(x, 3,4)$; should become z = x.reshape(3,4,order='F').copy() in NumPy.

## Customizing Your Environment

In MATLAB® the main tool available to you for customizing the environment is to modify the search path with the locations of your favorite functions. You can put such customizations into a startup script that MATLAB will run on startup.

NumPy, or rather Python, has similar facilities.

- To modify your Python search path to include the locations of your own modules, define the PYTHONPATH environment variable.
- To have a particular script file executed when the interactive Python interpreter is started, define the PYTHONSTARTUP environment variable to contain the name of your startup script.

Unlike MATLAB®, where anything on your path can be called immediately, with Python you need to first do an 'import' statement to make functions in a particular file accessible.

For example you might make a startup script that looks like this (Note: this is just an example, not a statement of "best practices"):

```
# Make all numpy available via shorter 'np' prefix
import numpy as np
# Make all matlib functions accessible at the top level via M.func()
import numpy.matlib as M
# Make some matlib functions accessible directly at the top level via, e.g. rand(3,3)
from numpy.matlib import rand,zeros,ones,empty,eye
# Define a Hermitian function
def hermitian(A, **kwargs):
    return np.transpose(A,**kwargs).conj()
# Make some shortcuts for transpose,hermitian:
# np.transpose(A) --> T(A)
# hermitian(A) --> H(A)
T = np.transpose
H = hermitian
```


## Links

See http://mathesaurus.sf.net/ (http://mathesaurus.sf.net/) for another MATLAB®/NumPy cross-reference.
An extensive list of tools for scientific work with python can be found in the topical software page (https://scipy.org/topicalsoftware.html).

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